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University of Science and Technology of China, Hefei, Anhui, P.R.China

Coauthors: Iryna Volodymyrivna Komashynska and Hussam Rabbaia

## ON PROPERTIES OF SYSTEMS OF LINEAR DIFFERENCE EQUATIONS

ALI MAHMUD ATEIWI

Consider a system of linear difference equations with variable coefficients

(1) where  $n = 0, 1, 2, \dots$ ,  $x_n$  is a vector from the Euclidean space  $\mathbb{R}^d$  and  $A_n$  is a  $d \times d$  matrix of coefficient. We assume that  $E + A_n$  is nondegenerate for all  $n \geq 0$ . So system (1) has the unique solution. We study the problem of reduction of the system (1) to a system with constant coefficients.  $Y_{n+1} = y_n + B_n y_n$ , (2) Where  $B$  is a constant matrix. Definition 1. A linear difference system is called reducible if there exists a Lyapunov transformation that reduces it to a system with constant coefficients (2). We establish reducibility conditions. Theorem 1. The linear difference system (1) is reducible if and only if a certain fundamental matrix  $X_n$  of it is representable in the form (3) Where  $E$  is the  $d \times d$  identity matrix and  $B$  is a certain constant  $d \times d$  matrix.

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DEPARTMENT OF MATHEMATICS AND STATISTICS, FACULTY OF SCIENCE, AL-HUSSEIN BIN TALAL UNIVERSITY

*E-mail address:* [ateiwi@hotmail.com](mailto:ateiwi@hotmail.com)